

Aufgabe I.2.3

a) Halbwellensymmetrie und ungerade. Aus diesem Grund reicht es, von 0 bis $\frac{t_p}{4}$ zu integrieren.

$$\begin{aligned}
 b_\mu &= \frac{8}{t_p} \int_0^{\frac{t_p}{6}} \frac{6\hat{i}}{t_p} t \sin(2\pi\mu f_0 t) dt + \frac{8}{t_p} \int_{\frac{t_p}{6}}^{\frac{t_p}{4}} \hat{i} \sin(2\pi\mu f_0 t) dt \\
 &= \frac{48\hat{i}}{t_p^2} \left[\frac{\sin(2\pi\mu f_0 t)}{(2\pi\mu f_0 t)^2} - t \frac{\cos(2\pi\mu f_0 t)}{2\pi\mu f_0 t} \right]_0^{\frac{t_p}{6}} + \frac{8\hat{i}}{t_p 2\pi\mu f_0} \left[-\cos(2\pi\mu f_0 t) \right]_{\frac{t_p}{6}}^{\frac{t_p}{4}} \\
 &= \frac{12\hat{i}}{\pi^2 \mu^2} \left[\sin(2\pi\mu f_0 t) - t 2\pi\mu f_0 \cos(2\pi\mu f_0 t) \right]_0^{\frac{t_p}{6}} + \frac{4\hat{i}}{\pi \mu} \left[\cos(2\pi\mu f_0 t) \right]_{\frac{t_p}{6}}^{\frac{t_p}{4}} \\
 &= \frac{12\hat{i}}{\pi^2 \mu^2} \left(\sin\left(\frac{\pi\mu}{3}\right) - \frac{\pi\mu}{3} \cos\left(\frac{\pi\mu}{3}\right) \right) + \frac{4\hat{i}}{\pi \mu} \left(\cos\left(\frac{\pi\mu}{3}\right) \right) \\
 &= \frac{12\hat{i}}{\pi^2 \mu^2} \sin\left(\frac{\pi\mu}{3}\right)
 \end{aligned}$$

b) $B_\mu = |b_\mu| \rightarrow \frac{12\hat{i}}{\pi^2 \mu^2} \left| \sin\left(\frac{\pi\mu}{3}\right) \right|$

$$\varphi_\mu = 0$$

c) $\underline{c}_0 = a_0 = 0$

$$\underline{c}_\mu = -j \frac{b_\mu}{2} = -j \frac{6\hat{i}}{\pi^2 \mu^2} \sin\left(\frac{\pi\mu}{3}\right)$$

d) $|c_\mu| = \frac{6\hat{i}}{\pi^2 \mu^2} \left| \sin\left(\frac{\pi\mu}{3}\right) \right| e^{-j\pi}$