

Aufgabe I.2.4

a) $f_b = 2f_1 = 2f_0 \rightarrow t_p = \frac{1}{f_0} = \frac{1}{f_a} = \frac{2}{f_b}$ $u_p(t) = \underbrace{\hat{u}_a}_{a_1} \cos(2\pi f_0 t) + \underbrace{\hat{u}_b}_{a_2} \cos(2\pi 2f_0 t)$

$$\underline{c}_\mu = \frac{a_\mu - jb_\mu}{2} ; \underline{c}_1 = \frac{a_1}{2} = \frac{\hat{u}_a}{2} \rightarrow \underline{c}_1 = \underline{c}_1^* = \frac{\hat{u}_a}{2} ; \underline{c}_2 = \frac{a_2}{2} = \frac{\hat{u}_b}{2} \rightarrow \underline{c}_2 = \underline{c}_2^* = \frac{\hat{u}_b}{2}$$

$$u_p(t) = \underbrace{\frac{\hat{u}_b}{2} \cdot e^{-j2\pi 2f_0 t}}_{\text{negative Frequenzen}} + \underbrace{\frac{\hat{u}_a}{2} \cdot e^{-j2\pi f_0 t}}_{\text{positive Frequenzen}} + \underbrace{\frac{\hat{u}_a}{2} \cdot e^{j2\pi f_0 t}}_{\text{positive Frequenzen}} + \underbrace{\frac{\hat{u}_b}{2} \cdot e^{j2\pi 2f_0 t}}_{\text{negative Frequenzen}}$$

b) $f_b = \frac{3}{2}f_a \rightarrow f_b = 3f_0, f_a = 2f_0$ $u_p(t) = \underbrace{\hat{u}_a}_{a_2} \cos(2\pi 2f_0 t) + \underbrace{\hat{u}_b}_{a_3} \cos(2\pi 3f_0 t)$

$$\underline{c}_2 = \frac{\hat{u}_a}{2} \rightarrow \underline{c}_2^* = \frac{\hat{u}_a}{2} ; \underline{c}_3 = \frac{\hat{u}_b}{2} \rightarrow \underline{c}_3^* = \frac{\hat{u}_b}{2}$$

$$u_p(t) = \underbrace{\frac{\hat{u}_b}{2} \cdot e^{-j2\pi 3f_0 t}}_{\underline{c}_3^*} + \underbrace{\frac{\hat{u}_a}{2} \cdot e^{-j2\pi 2f_0 t}}_{\underline{c}_2^*} + \underbrace{\frac{\hat{u}_a}{2} \cdot e^{j2\pi 2f_0 t}}_{\underline{c}_2} + \underbrace{\frac{\hat{u}_b}{2} \cdot e^{j2\pi 3f_0 t}}_{\underline{c}_3}$$